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One-sided device-independent random number generation through fiber channels

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Abstract

Randomness is an essential resource and plays important roles in various applications ranging from cryptography to simulation of complex systems. Certified randomness from quantum process is ensured to have the element of privacy but usually relies on the device's behavior. To certify randomness without the characterization for device, it is crucial to realize the one-sided device-independent random number generation based on quantum steering, which guarantees security of randomness and relaxes the demands of one party's device. Here, we distribute quantum steering between two distant users through a 2 km fiber channel and generate quantum random numbers at the remote station with untrustworthy device. We certify the steering-based randomness by reconstructing covariance matrix of the Gaussian entangled state shared between distant parties. Then, the quantum random numbers with a generation rate of 7.06 Mbits/s are extracted from the measured amplitude quadrature fluctuation of the state owned by the remote party. Our results demonstrate the first realization of steering-based random numbers extraction in a practical fiber channel, which paves the way to the quantum random numbers generation in asymmetric networks.

Introduction

The random number has broad applications in many fields, ranging from simulation, cryptography, as well as computer networks or lotteries^{1,2}. The randomness and its privacy require assumptions about the computational power of the adversary, which motivates the extensive study of true random number generators based on some unpredictable physical processes³. As a typical case of true random numbers, quantum random numbers have attracted much attention since the inherent randomness of measurement outputs in quantum mechanics is guaranteed by Born's rule⁴. For instance, random numbers can be generated by detecting single photons after they pass through a balanced beam-splitter⁵, which relies on the device working in a particular way. However, deviations in the device behavior can affect

the randomness of outputs and are difficult to detect, and any real device is too complicated to model in its entirety, which will leave open the possibility that an adversary can exploit a feature of the device outside the model, leading to the insecurity of generated random numbers⁶.

This problem can be tackled by verifying Bell non-locality⁷ or Einstein-Podolsky-Rosen (EPR) steering⁸ between distant users. The violation of Bell inequality ensures the quantum random number generation (QRNG) in a device-independent manner^{9–13}, where the user's devices are all untrusted. Different from Bell nonlocality, EPR steering can be used to realize one-sided device-independent (ISDI) QRNG, where only the device of steering party is untrusted since it is an asymmetric form of correlation that lies between entanglement¹⁴ and Bell nonlocality¹⁵ hierarchically. Such a ISDI scenario typically allows users to own asymmetric devices, for instance, the bank and its clients where the bank owns trustworthy devices but the clients only have cheap and untrustworthy devices¹⁶. Furthermore, in a practical scenario, not all users involved in the network might have the ability to prepare the required quantum resources, especially for some remote untrusted users. In this case, entanglement

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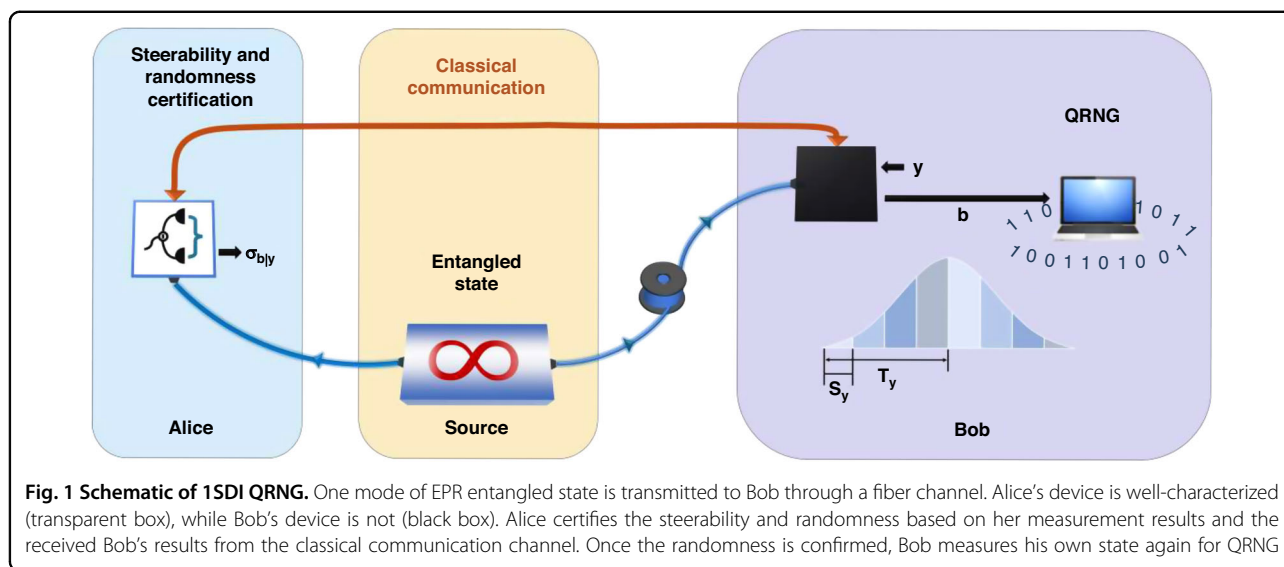


Fig. 1 Schematic of 1SDI QRNG. One mode of EPR entangled state is transmitted to Bob through a fiber channel. Alice’s device is well-characterized (transparent box), while Bob’s device is not (black box). Alice certifies the steerability and randomness based on her measurement results and the received Bob’s results from the classical communication channel. Once the randomness is confirmed, Bob measures his own state again for QRNG

resources can be prepared in a quantum server and distributed to remote users. Considering the practical channel loss and noise, how to verify the security and efficiency of the generated random numbers based on the shared quantum correlations remains a challenge.

Several experiments have implemented the randomness certification by allowing source or measurement devices to be partially characterized in the discrete variable system^{17–22}. The deterministic preparation of continuous variable (CV) system benefits quantum random number generation²³. For example, some source-device-independent protocols in CV systems can reach a higher generation rate while removing the assumption about the source for bounding the side information^{24–26}. Recently, a protocol of certifying the steering-based randomness in a CV system is demonstrated in a proof-of-principle experiment²⁷. Towards practical applications, it is essential to certify randomness and extract quantum random numbers in a remote station based on the shared EPR steering.

In this work, we demonstrate the distribution of CV EPR steering over a 2 km fiber channel and extract quantum random numbers after the certification of randomness. What’s more important, the random numbers are generated in the remote station without any assumptions about its device, observing the first steering-based random number extraction resisting the actual loss and noise. By reconstructing the covariance matrix (CM) of the shared entangled state with homodyne detection, the nonzero randomness is verified at the local station. The quantum random numbers with a generation rate of 7.06 Mbits/s are extracted from the measured amplitude quadrature fluctuation of the state owned by the remote party and pass the randomness statistical test suite. Our experiment presents an application of distributed CV EPR

steering in fiber channel and makes a key step towards generating quantum random numbers for future network protocols^{28,29}.

Results

Theoretical framework

As shown in Fig. 1, the 1SDI scenario we considered is close to the actual situation where only the device of local user, named Alice, is well-characterized (transparent box), while the device of the remote user, named Bob, is not (black box). One mode of a CV EPR entangled state is transmitted to Bob through a fiber (quantum) channel, while the other mode is kept by Alice. The whole protocol contains three steps: Step-I, EPR steering verification, where Alice and Bob verify the distributed steerability by measuring their own states; Step-II, randomness certification, where Alice verifies the steering-based randomness; Step-III, quantum random number extraction in Bob’s station, by measuring his own state when Alice confirms the validity of steering-based randomness.

To be more specific, in the step-I, Alice and Bob perform a series of quadrature measurements on their own optical modes respectively and Bob sends his measurement results to Alice through the classical channel. Alice verifies the steerability based on the reconstructed CM from their measurement results (see details in Materials and methods). The quadrature operators of each mode are denoted by $\hat{q}_i = \hat{a}_i^\dagger + \hat{a}_i$ and $\hat{p}_i = i(\hat{a}_i^\dagger - \hat{a}_i)$, where \hat{a}_i^\dagger and \hat{a}_i are the creation and annihilation operators and satisfy the canonical commutation relations $[\hat{a}_j, \hat{a}_k^\dagger] = 2\delta_{jk}$. Since the distributed entangled state and the measurements both have Gaussian nature, the entanglement properties of such system can be described by its CM with elements $\sigma_{ij} = \langle \hat{R}_i \hat{R}_j + \hat{R}_j \hat{R}_i \rangle / 2 - \langle \hat{R}_i \rangle \langle \hat{R}_j \rangle$, where the vector $\hat{R} = (\hat{q}_A, \hat{p}_A, \hat{q}_B, \hat{p}_B)^\top$ collects the quadrature operators

for both modes. The steerability from Bob to Alice can be quantified by the parameter

$$\mathcal{G}^{B \rightarrow A} = \max \left\{ 0, \frac{1}{2} \ln \frac{\text{Det } \sigma_B}{\text{Det } \sigma_{AB}} \right\} \quad (1)$$

where σ_B and σ_{AB} denote the CM for the reduced mode \hat{B} , and the group $(\hat{A}\hat{B})$, respectively³⁰. This quantity is a monotone under Gaussian local operations and classical communication and vanishes if and only if the state described by its covariance matrix is nonsteerable by Gaussian measurements. Once the steerability from Bob to Alice exists, the probability that Bob will obtain the results for his measurement cannot be explained by a local deterministic distribution, resulting in intrinsic randomness among his outcomes.

In the step-II, Alice estimates the amount of randomness based on the conditional states for Bob's specific measurements and outcomes. The outcomes of a homodyne detection, however, are continuous form over the whole phase space and cannot be directly used for randomness certification, so we bin them into a finite number of outcomes by utilizing the periodic coarse-grained protocol³¹, as follows:

$$\begin{aligned} M_{b|y} &= \int_{\mathbb{R}} f_b(z, T_y) |z\rangle_y \langle z| dz \\ f_b(z, T_y) &= \begin{cases} 1, & bs_y \leq z \bmod T_y < (b+1)s_y \\ 0, & \text{otherwise} \end{cases} \end{aligned} \quad (2)$$

Here the measurements y performed by Bob are characterized as positive-operator-valued measures (POVMs) with finite elements $M_{b|y}$, where the outcomes $b \in \{0, 1, \dots, o_B - 1\}$, $y \in \{\hat{q}, \hat{p}\}$ and $|z\rangle_y$ are the corresponding eigenstates. The periodic protocol defined by the periodic mask function is parameterized by the period T_y with o_B outcomes and bin width $s_y = T_y/o_B$, as illustrated in Fig. 1. After the strategy for binning Bob's results is determined, full information of the conditional states $\sigma_{b|y}^{\text{obs}}$ in Alice can be obtained from the reconstructed CM, as the CM contains all relevant information of the Gaussian state shared between them. The set of conditional states is called assemblage, and one can certify randomness associated with Bob's measurement outcomes through the analysis of it³². To be specific, the figure of merit we use to quantify the amount of randomness is the maximal probability $P_g(y^*)$ that an eavesdropper (Eve) correctly predicts the outputs when she knows the input y^* and any other available side information, which can be formulated as a semidefinite

program (SDP):

$$\max_{\sigma_{b|y}^e} P_g(y^*) = \text{Tr} \left[\sum_e \sigma_{b=e|y^*}^e \right] \quad (3a)$$

$$\text{s.t. } \sum_e \sigma_{b|y}^e = \sigma_{b|y}^{\text{obs}}, \forall b, y \quad (3b)$$

$$\sum_b \sigma_{b|y}^e = \sum_b \sigma_{b|y'}^e, \forall e, y \neq y' \quad (3c)$$

$$\sigma_{b|y}^e \geq 0, \forall b, y, e \quad (3d)$$

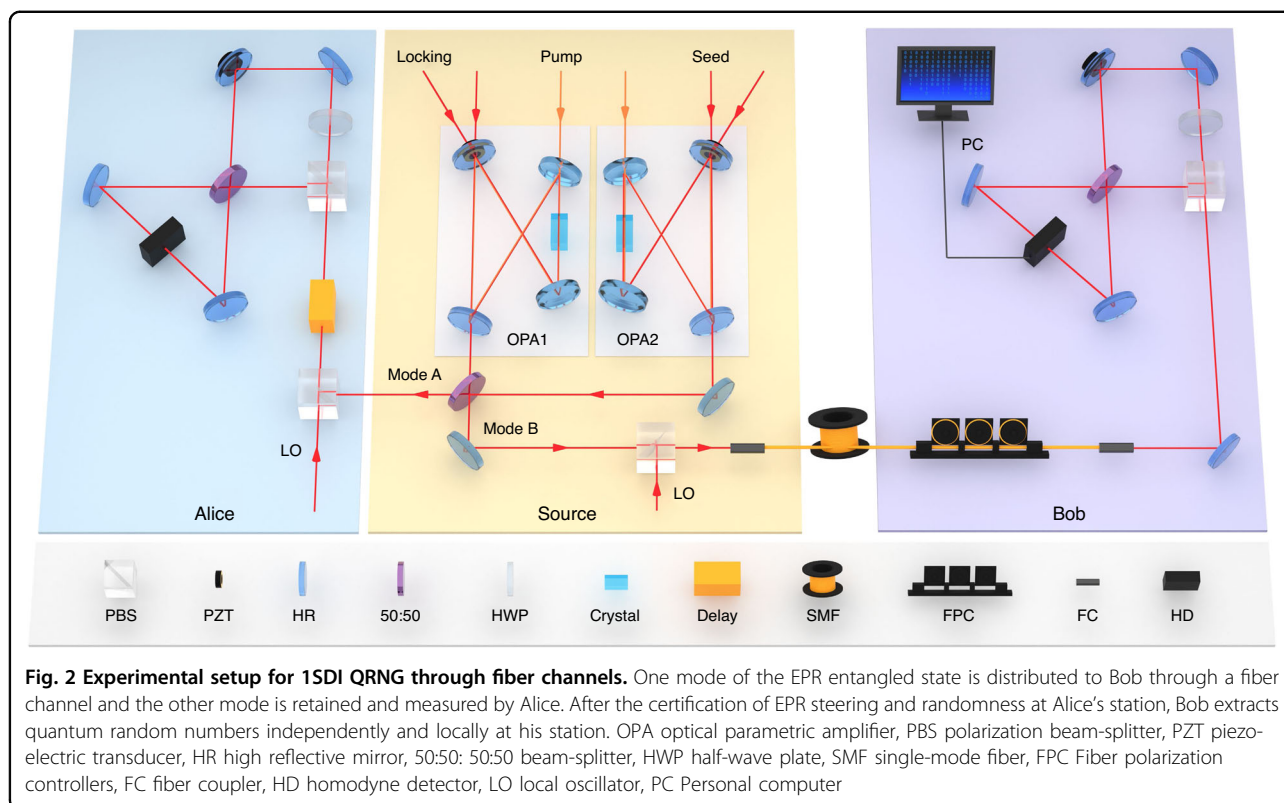
Therefore, the amount of randomness generated by Bob's outcomes is quantified by the min-entropy³³ $H_{\min}(y^*) = -\log_2 P_g(y^*)$.

Moreover, instead of full quantum state characterization, we can also certify randomness based on the joint probability distribution between Alice and Bob's limited measurements. The joint probability distribution $p^{\text{obs}}(ab|xy)$ can be derived from the reconstructed CM when only a few measurement directions at Alice's side are considered. The protocol of randomness certification based on the joint probability distribution is presented²⁷, by replacing Eq. (3b) with $\sum_e \text{Tr}[M_{a|x} \sigma_{b|y}^e] = p^{\text{obs}}(ab|xy), \forall a, b, x, y$, for known elements $M_{a|x}$ of POVMs of Alice. It also guarantees that Eve's strategy is compatible with the observed probabilities.

In the step-III, Bob extracts quantum random numbers independently and locally at his station once Alice confirms that the steering-based randomness exists. Bob performs homodyne detection again to measure the fluctuations of amplitude or phase quadrature of his own optical mode and extract quantum random numbers from a large amount of measured fluctuations.

The experiment

The schematic of the experimental setup of 1SDI QRNG is illustrated in Fig. 2. We generate the squeezed state of light at 1550 nm by using an optical parametric amplifier (OPA), which is a bow-tie traveling-wave cavity consisting of two plane mirrors, two concave mirrors, and a type-0 periodically poled potassium titanyl phosphate (PPKTP) crystal with a length of 10 mm. By controlling the relative phase difference between the pump and seed beams to zero, a quadrature phase squeezed state is obtained from the OPA. Two squeezed states with -2.78 dB/ $+3.47$ dB and -2.69 dB/ $+3.47$ dB squeezing/antisqueezing are prepared from OPA1 and OPA2, respectively. These squeezing levels of generated states are mainly limited by the normalized pump power and escape efficiency of the OPA, as well as the total detection



efficiency. More details are given in Materials and methods. As purity of the squeezed state is more important for the amount of generated randomness than squeezing level, the pump power of OPAs is 20 mW which can achieve the highest squeezing purity in our experiment. The CV EPR entangled state is obtained by coupling these two phase squeezed states on a 50:50 beam splitter with a relative phase difference of $\pi/2$.

In the distribution of the EPR state, the polarization multiplexing technique is applied to transmit one mode of the EPR state and local oscillator (LO) through one fiber. The mode \hat{B} of the CV EPR state with vertical polarization and a LO with horizontal polarization are coupled on a polarization beam-splitter (PBS) and the output is transmitted to Bob through a single-mode fiber (SMF) channel. After the transmission, the mode \hat{B} and the LO are separated by a PBS at Bob's station to implement the homodyne detection.

The most challenging part in the distribution of EPR steering is the synchronization of two EPR entangled modes owned by Alice and Bob. Only the photons generated simultaneously present the highest quantum correlation, once the time delay between two photons exceeds the coherence time, the quantum correlation will decrease and even disappear. Thus, it is important to synchronize the photons in Alice's and Bob's station in

the experiment. To do so, we transmit the EPR mode owned by Alice through the same fiber length (Delay in Fig. 2) to make sure the maximum quantum correlation is observed between Alice's and Bob's modes.

In the experiment of step-I, Alice and Bob measure the amplitude and phase quadratures of their own optical modes simultaneously and record the output of the homodyne detectors by a digital-storage oscilloscope with a sampling rate of 10 MS/s. Here, time-domain data is acquired by demodulating output signals of the homodyne detector at a sideband frequency of 4 MHz within a 300 kHz bandwidth and amplified 200 times via a low noise preamplifier. After the measurement, Bob sends his results of amplitude and phase quadrature of mode \hat{B} to Alice through the classical channel. Alice reconstructs the CM based on both Bob's and her measurement results and verifies the steerability from Bob to Alice.

In the experiment of step-II, after the verification of EPR steering, Alice quantifies the amount of certifiable randomness with the optimized periodic coarse-grained protocol. As the state we generated is not pure, we choose the binning periods $T_{\hat{p}} = T_{\hat{q}}$ for Bob's two quadrature measurements $\{\hat{p}, \hat{q}\}$, which provides higher randomness than the case satisfying mutual-unbiasedness condition³¹, i.e., $T_{\hat{p}} = 2\pi\sigma_B/T_{\hat{q}}$. Within the chosen binning periods, we bin their outputs into $o_B = 32$ outcomes,

corresponding to a fixed bits combination of length 5 assigned to each sample point³. Each outcome is associated with a conditional state $\sigma_{b|y}^{\text{obs}}$ at Alice's side, which can be obtained from the reconstructed CM. As we mentioned before, the condition (3b) can be replaced by the joint probabilities with Alice's limited measurements. We further bin the outputs of four measurement directions $\{\hat{p}_A, (\hat{p}_A + \hat{q}_A)/\sqrt{2}, (\hat{p}_A - \hat{q}_A)/\sqrt{2}, \hat{q}_A\}$. The output of each measurement is binned into $o_A = 32$ outcomes, $o_A - 1$ of which divides the range $[-5, 5]$ evenly, and the last bin constitutes everything outside this range. For each coarse-grained protocol, one can describe the measurements $M_{a|x}, M_{b|y}$ performed by Alice and Bob. Based on the reconstructed CM, the conditional states $\sigma_{b|y}^{\text{obs}} = \text{Tr}_B[I \otimes M_{b|y}\rho]$ of Alice as well as the joint probability distribution $p^{\text{obs}}(ab|xy)$ are obtained. Hence the randomness can be certified as described in Eq. (3).

In the experiment of step-III, to extract quantum random numbers, Bob measures the amplitude quadrature of his own mode using a homodyne detector when Alice confirms the existence of randomness. Since the distribution of the measured amplitude fluctuation of the EPR mode is Gaussian rather than a uniform distribution, the raw random data cannot pass any randomness statistical tests³⁴. To eliminate the classical effects and improve the statistical quality of quantum random numbers, we apply the Toeplitz hashing³⁴. Here we acquire 1 Tbits raw data and extract 1 Gbits random numbers by Toeplitz matrix. Finally, these extracted random numbers are evaluated by using the standard randomness statistical test suite.

Experimental results

The result of EPR steering verification in the step-I is shown in Fig. 3a, where the Gaussian steerabilities $\mathcal{G}^{B \rightarrow A}$ for different transmission distances in the fiber channel are presented. The curves represent theoretical predictions based on the entangled state, which is generated by mixing two squeezed states originating from OPA1 and OPA2 on a balanced beam splitter. Additionally, the effect of fiber channel loss is also considered in the theoretical predictions by adopting the noisy channel described in the Materials and methods. It is obvious that the steerability decreases with the increase of transmission distance. The presence of the steerability from Bob to Alice guarantees the success of the whole protocol.

According to different coarse-grained protocols, we substitute the corresponding conditional states $\sigma_{b|y}^{\text{obs}}$ into Eq. (3) and obtain the randomness for different transmission distances (blue curve) in the step-II, as shown in Fig. 3b. As previously explained, we also compare the randomness with limited four measurement directions $\{\hat{p}_A, (\hat{p}_A + \hat{q}_A)/\sqrt{2}, (\hat{p}_A - \hat{q}_A)/\sqrt{2}, \hat{q}_A\}$ on Alice's side (red curve). The randomness derived from limited

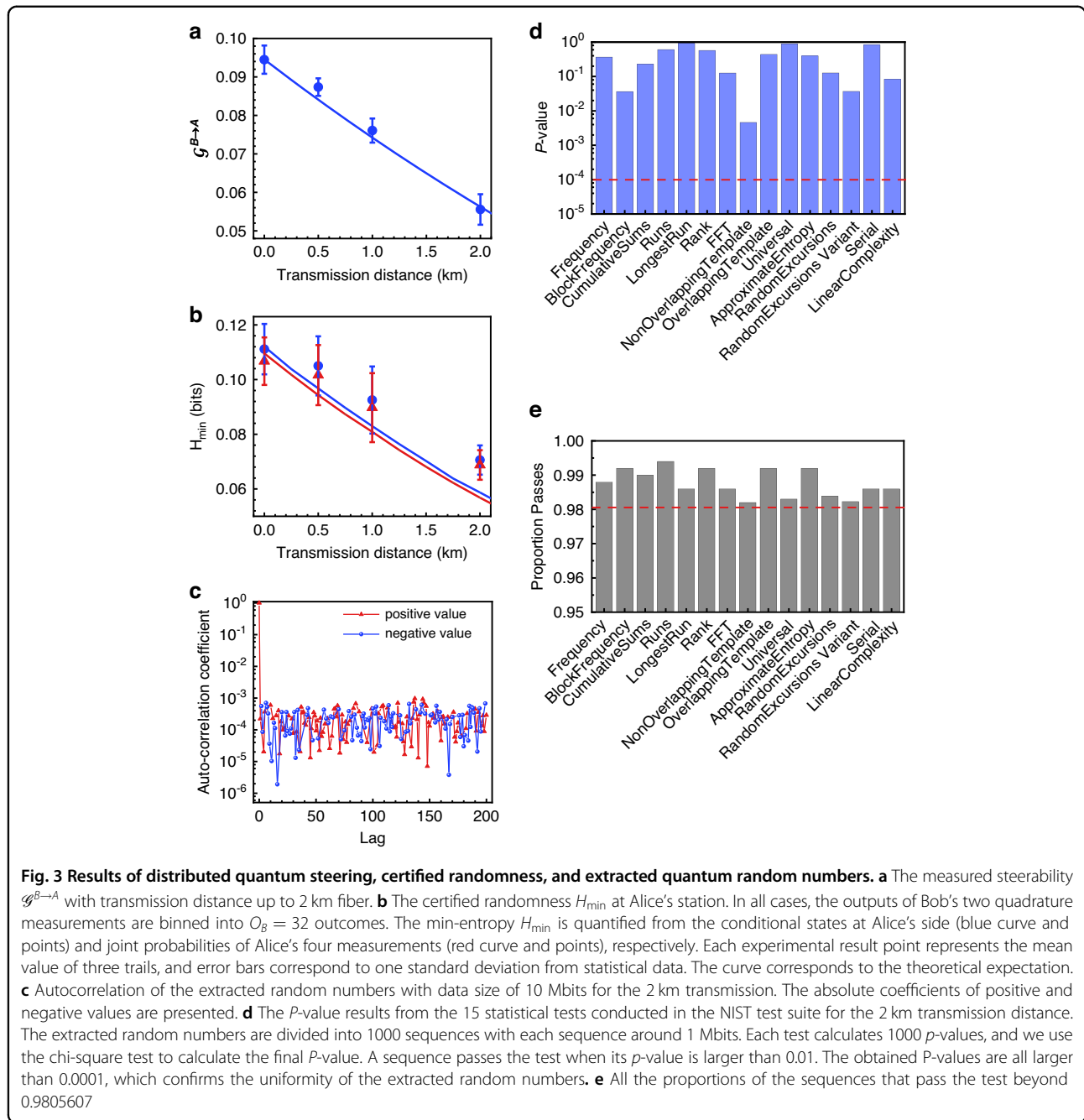
measurements is slightly lower than those achieved through conditional states. Nonetheless, the overall trend remains consistent, that is, the amount of certifiable randomness H_{\min} decreases as the transmission distance increases.

In the extraction of random numbers at Bob's station, due to the difficulty of directly processing a long raw data sequence, we split the 1 Tbit raw random sequence into several n -bit-long blocks and process them individually³⁵. For each block of raw data, we employ an $n \times m$ Toeplitz matrix as an extractor, where $n + m - 1$ pre-stored seeds true random bits are used to construct the Toeplitz matrix and m random bits are extracted by multiplying the Toeplitz matrix with n raw bits. For a transmission distance of 2 km, the randomness H_{\min} is certified to be 0.07057 bits per sample. Consequently, we choose $m = 1024$ and $n = 72,600 > m \times 5 / 0.07057 = 72,552$ to generate the corresponding extracted random bits^{23,34}, and obtain the quantum random numbers with a generation rate of 7.06 Mbits/s (see Table 1 for a summary of the QRNG demonstrations based on entangled states). Additionally, the generation rates of random numbers at 0.002, 0.5, and 1 km fiber channels are 11.11, 10.5, and 9.25 Mbits/s respectively (see details in the Supplementary information), which are slightly higher than that in a 2 km fiber channel, as the certifiable randomness H_{\min} at these three transmission distances are larger.

After the extraction of the quantum random numbers, we analyze the autocorrelation coefficients on the post-processed random numbers at a transmission distance of 2 km, as depicted in Fig. 3c. It can be found that the autocorrelation coefficients consistently approach zero at different time lags, with an average value of 1.28×10^{-5} . Finally, we test the extracted random numbers with the NIST test suite, which comprises 15 different tests. For these tests, we divide the extracted random numbers into 1000 sequences. The results of the NIST test suite for random bits at transmission distances of 2 km are presented in Fig. 3d, e, and the results at the other three transmission distances are given in Supplementary information. All the P -values exceed 0.0001, which demonstrates that the extracted random numbers satisfy a uniform distribution. The proportion passes of all sequences fall within the confidence interval of 0.99 ± 0.0094392 , providing a strong evidence of the randomness of Bob's outcomes.

Discussion

In summary, we experimentally demonstrate the 1SDI QRNG based on the distributed deterministic CV quantum steering through a 2 km fiber channel. By reconstructing its covariance matrix, we verify the steerability from Bob to Alice at Alice's station first. Then the randomness is certified in the 1SDI scenario where the



remote user lacks the ability to prepare quantum state and makes no additional assumptions about the device. Once the randomness exists, we extract the quantum random numbers locally at Bob's station by measuring the fluctuations of his own optical mode. The quantum random numbers with a generation rate of 7.06 Mbits/s are achieved at Bob's station which is 2 km away from the entanglement source.

The demonstrated protocol can be generalized to the quantum networks involving multiple users, where only a few users own trustworthy devices while the

untrustworthy devices are used for the most users. The multipartite scenario can bring diverse structures and properties of the distributed steering, and hence additional protection against possible attacks can be found³⁶. The transmission distance can be extended by further enhancing squeezing purity and reducing channel loss and excess noise. For instance, by enhancing squeezing purity, the transmission distance can be further improved to 11.42 km within the current experimental feasibility, since up to -10 dB/ $+11$ dB of squeezing/antisqueezing has been demonstrated³⁷. The

Table 1 Generation rates of QRNG demonstrations based on entangled states

QRNG	Type	DoF	Generation rate
39			1.5×10^{-5} bits/s
40			0.4 bits/s
11	DI	DV	114 bits/s
41			13.5 kbits/s
42			3.6 kbits/s
22	SDI	DV	4 Mbits/s
This work	1SDI	CV	7.06 Mbits/s

DI Device independent, SDI Source-device independent, 1SDI One-sided device-independent, DoF Degree of freedom used to encode information

presented results make a key step toward the application of EPR steering in the 1SDI scenario and have potential applications in fiber-based quantum networks.

Materials and methods

Details of experiment

The laser source employed in our experiment is a 1550 nm fiber laser (NKT Photonics). The OPA, which is in a bow-tie configuration, consists of a type 0 PPKTP crystal ($1 \times 2 \times 10$ mm³), two plane mirrors, and two concave mirrors with $r = 50$ mm. Both the front and rear faces of the crystal are anti-reflectivity coated for both wavelengths to reduce the intra-cavity losses. A piezo-actuated plane mirror is used as the input mirror for the seed beam and locking beam, which is coated with high reflectivity (HR) at 1550 nm and 775 nm. The other plane mirror is used as the output mirror, which has a partial reflectivity of $87.5\% \pm 1\%$ for 1550 nm and HR for 775 nm. The pump beam is coupled into the OPA through a concave mirror, which is HR for 1550 nm and has a 80% reflectivity for 775 nm. The other concave mirror is HR for both wavelengths. The cavity length and linewidth of the OPA are about 478 mm and 12.3 MHz, respectively. For performing the measurements, we carefully adjust the OPA to the desired state through mode matching, temperature control, gain adjustment, and phase locking to ensure the stability of the squeezing source.

To lock the cavity of the OPA, a counter-propagating locking beam carrying on a phase modulation signal of 16.67 MHz is injected into the OPA through the input mirror with PZT. By detecting the transmitted locking beam with a photodetector and feed-backing the demodulated error signal to the PZT on the input mirror, the cavity length is stabilized. The relative phase difference between the seed and pump beams of the OPA is actively stabilized to 0° by feed-backing the error signal, which is obtained from the interference signal of the seed and down-converted beams to a PZT-mounted mirror in the path of the seed beam. After locking the cavity and relative

phase difference, a phase-squeezed state is deterministically prepared. For the homodyne detector, the seed beam power is 100 μ W in the OPA and the LO power is 600 μ W. The variances of the squeezing and antisqueezing quadratures are measured with a total detection efficiency of 87%. Other related parameters for the measurement are given in the Supplementary Information.

The transmission efficiency of the fiber channel, denoted as η , is defined by $\eta = \eta_0 \times 10^{-\alpha L/10}$, where $\eta_0 = 0.9$ represents the fiber coupling efficiency, L is the length of fiber transmission, and α is the loss coefficient of the SMF, typically ~ 0.2 dB/km at 1550 nm. Here the modes transmitted through the noisy channel are

$$\begin{aligned}\hat{q}_i^{\text{out}} &= \sqrt{\eta}\hat{q}_i^{\text{in}} + \sqrt{1-\eta}(\hat{q}_N + \hat{q}_\nu) \\ \hat{p}_i^{\text{out}} &= \sqrt{\eta}\hat{p}_i^{\text{in}} + \sqrt{1-\eta}(\hat{p}_N + \hat{p}_\nu)\end{aligned}\quad (4)$$

where the subscripts N and ν represent the noise and vacuum state respectively. The excess noise in the fiber channel is given by $\delta = \Delta^2 \hat{q}_N = \Delta^2 \hat{p}_N$. The power of the local oscillator distributed in the fiber channel is set to 0.6 mW, which leads to the excess noise of $\delta = 0.01$ shot-noise-unit in our experiment.

In the process of extraction, to obtain the seed sequence for the Toeplitz hashing extractor, we discretize the probability distribution of the measured amplitude fluctuations of mode \hat{B} into the binary raw data first. Then we choose 50 Mbits data and feed them to the SHA-512 function. In this way, we obtain the seed sequence of 0.22 Mbits.

Reconstruction of the covariance matrix

The CM of the EPR entangled state can be partially characterized as (assuming the cross-correlations between different quadratures are zero):

$$\sigma = \begin{bmatrix} \Delta^2 \hat{q}_A & 0 & C(\hat{q}_A, \hat{q}_B) & 0 \\ 0 & \Delta^2 \hat{p}_A & 0 & C(\hat{p}_A, \hat{p}_B) \\ C(\hat{q}_A, \hat{q}_B) & 0 & \Delta^2 \hat{q}_B & 0 \\ 0 & C(\hat{p}_A, \hat{p}_B) & 0 & \Delta^2 \hat{p}_B \end{bmatrix}$$

where $\Delta^2 \hat{q}_A$, $\Delta^2 \hat{p}_A$, $\Delta^2 \hat{q}_B$, $\Delta^2 \hat{p}_B$ represent the variances of amplitude and phase quadratures of EPR entangled modes \hat{A} and \hat{B} , respectively, which are obtained from the measured $\hat{q}_{A(B)}$ and $\hat{p}_{A(B)}$ in time domain. $C(\hat{q}_A, \hat{q}_B)$ and $C(\hat{p}_A, \hat{p}_B)$ represent cross-correlations between the output optical modes and are calculated based on the measured variances with the following relations³⁸:

$$\begin{aligned}C(\hat{R}_i, \hat{R}_j) &= \frac{1}{2}[\Delta^2(\hat{R}_i + \hat{R}_j) - \Delta^2 \hat{R}_i - \Delta^2 \hat{R}_j] \\ C(\hat{R}_i, \hat{R}_j) &= -\frac{1}{2}[\Delta^2(\hat{R}_i - \hat{R}_j) - \Delta^2 \hat{R}_i - \Delta^2 \hat{R}_j]\end{aligned}$$

When the transmission distances between the source and Bob are 0.002, 0.5, 1, and 2 km, the reconstructed

CMs of the EPR entangled state are:

$$\begin{bmatrix} 1.35 \pm 0.01 & 0 & 0.77 \pm 0.01 & 0 \\ 0 & 1.36 \pm 0.01 & 0 & -0.79 \pm 0.01 \\ 0.77 \pm 0.01 & 0 & 1.38 \pm 0.01 & 0 \\ 0 & -0.79 \pm 0.01 & 0 & 1.33 \pm 0.01 \end{bmatrix}$$

$$\begin{bmatrix} 1.32 \pm 0.01 & 0 & 0.73 \pm 0.02 & 0 \\ 0 & 1.35 \pm 0.01 & 0 & -0.76 \pm 0.03 \\ 0.73 \pm 0.02 & 0 & 1.35 \pm 0.00 & 0 \\ 0 & -0.76 \pm 0.03 & 0 & 1.33 \pm 0.01 \end{bmatrix}$$

$$\begin{bmatrix} 1.32 \pm 0.00 & 0 & 0.73 \pm 0.01 & 0 \\ 0 & 1.34 \pm 0.01 & 0 & -0.74 \pm 0.01 \\ 0.73 \pm 0.01 & 0 & 1.35 \pm 0.00 & 0 \\ 0 & -0.74 \pm 0.01 & 0 & 1.32 \pm 0.01 \end{bmatrix}$$

$$\begin{bmatrix} 1.30 \pm 0.01 & 0 & 0.69 \pm 0.01 & 0 \\ 0 & 1.31 \pm 0.00 & 0 & -0.68 \pm 0.01 \\ 0.69 \pm 0.01 & 0 & 1.33 \pm 0.01 & 0 \\ 0 & -0.68 \pm 0.01 & 0 & 1.30 \pm 0.01 \end{bmatrix}$$

respectively.

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X.S., Q.He, and Y.X. conceived the original idea; J.Z., M.Z., and X.S. designed the experiment and carried out the experiment; Y.L. and Y.X. completed the theoretical analysis; J.Z. and Y.L. analyzed the data; D.H., J.L., and M.W. participated in part of the experiment. Q.H., Q.G., and X.S. managed the project. J.Z., Y.L., Y.X., X.S., and Q.H. prepared the paper.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Conflict of interest

The authors declare no competing interests.

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