Coherent manipulation of spin-wave vector for polarization of photons in an atomic ensemble

Shujing Li, Zhongxiao Xu, Haiyan Zheng, Xingbo Zhao, Yuelong Wu, Hai Wang,* Changde Xie, and Kunchi Peng

The State Key Laboratory of Quantum Optics and Quantum Optics Devices, Institute of Opto-Electronics, Shanxi University, Taiyuan 030006, People’s Republic of China

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We experimentally demonstrate the manipulation of two orthogonal components of a spin wave in an atomic ensemble. Based on Raman two-photon transition and Larmor spin precession induced by magnetic field pulses, the coherent rotations between the two components of the spin wave are controllably achieved. Successively, the two manipulated spin-wave components are mapped into two orthogonal polarized optical emissions. By measuring Ramsey fringes of the retrieved optical signals, the π/2-pulse fidelity of ~96% is obtained. The presented manipulation scheme can be used to build an arbitrary rotation for qubit operations in quantum information processing based on atomic ensembles.

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I. INTRODUCTION

The coherent manipulation of quantum states in memory elements plays an important role in quantum information processing (QIP) [1–3]. Atomic ensembles with the ability of collectively enhanced coupling to a definite light mode [2] can serve as good quantum memory elements and have attracted considerable attention in recent years [1–3]. By using techniques of electromagnetically induced transparency (EIT), the storage and retrieval of photon states have been successfully accomplished with atomic ensembles [2]. The coherent memory time has reached a 1-s time scale in a Bose-Einstein Condensation (BEC) ensemble via controlled nonlinear interactions [4]. Quantum memories for single spin-wave excitation created via Raman scattering or EIT storage in atomic ensembles have been demonstrated [5,6]. Recently, the experimental studies on collective qubit memory used to achieve the atom–photon entanglement have made great progress. In these studies [7–9], two orthogonal [7] or two spatially distinct [8] spin waves, or two atomic ensembles sharing a spin-wave excitation [9] are used to encode the long-time atomic qubit. The lifetime of qubit memory for optical lattice spin wave has reached 3 ms [7]. QIP schemes based on atomic ensembles such as the entanglement swapping [1], the multipartite entanglement of atomic ensembles [3,10], the controlled-NOT gate [10], and quantum computation with probabilistic quantum gates [11] have been proposed. In these proposed schemes, the memory qubits may be encoded in two orthogonal spin waves and single-bit operations are required. Single-qubit gate operations are the $R(\theta, \phi)$ and $R_z(\phi_z)$ rotations [12], which can be used to build an arbitrary rotation on the Bloch sphere. The single-qubit operations have been realized in a single ion [12], in trapped neutral atoms [13,14], or a quantum dot system [15], whereas they have not been demonstrated in atomic ensembles so far. The $R(\theta, \phi)$ and $R_z(\phi_z)$ rotations in a spin-wave basis are an important precondition to perform a single-qubit operation based on atomic ensemble. Recently, the experiment of the coherence transfer between two storage channels in BEC [4] has been realized. However, the required rotation of the spin wave for performing a single-qubit operation still has not been achieved.

II. THEORETICAL MODEL

Figures 1(a)–1(c) illustrate the $^{87}$Rb relevant levels involved in the storage, Raman manipulation, and read-out processes, where $|\uparrow\rangle = |S^z = 1, M_F = +1\rangle, |\downarrow\rangle = |S^z = 1, M_F = -1\rangle, |s\rangle = |S^z = 2, F = 2, M_F = +1\rangle, and |e\rangle = |S^2 = 2, F' = 1, M_F = 0\rangle$. Considering the atomic spin wave associated with the coherence between the state $|s\rangle$ and the superposition state $|\Phi\rangle = \alpha|\uparrow\rangle + e^{i\Delta}\beta|\downarrow\rangle$ ($|\alpha|^2 + |\beta|^2 = 1$), we introduce a collective, slowly varying atomic operator, appropriately averaged over a small but macroscopic volume with atomic numbers of $N_\zeta \gg 1$ at positions $z$ [16]; $\hat{p}_\Phi(z,t) = (N_\zeta)^{-1} \sum_{j=1}^{N_\zeta} |\Phi_j\rangle e^{i\omega_\Phi z}$. where $\omega_\Phi$ is the frequency of the transition $|s\rangle \leftrightarrow |\uparrow\rangle$. Introducing $|\Phi_j\rangle = \alpha|\uparrow_j\rangle + e^{i\Delta}\beta|\downarrow_j\rangle$ into the expression of $\hat{p}_\Phi(z,t)$, we have $\hat{p}_\Phi(z,t) = \alpha\hat{p}_{\uparrow}(z,t) + e^{-i\Delta}\beta\hat{p}_{\downarrow}(z,t)$, where $\hat{p}_{\uparrow}(z,t) = N_\zeta^{-1} \sum_{j=1}^{N_\zeta} |\uparrow_j\rangle\langle\uparrow_j| e^{i\omega_\Phi z}$ and $\hat{p}_{\downarrow}(z,t) = N_\zeta^{-1} \sum_{j=1}^{N_\zeta} |\downarrow_j\rangle\langle\downarrow_j| e^{i\omega_\Phi z}$ are the two spin-coherence operators, the real numbers $\alpha$ ($|\alpha|^2$) and $\beta$ ($|\beta|^2$) can be regarded as coherence amplitudes (populations) of the $\hat{p}_{\uparrow}(z,t)$ and $\hat{p}_{\downarrow}(z,t)$ components, respectively; $\Delta$ is the relative phase between them. The atomic spin-wave operators $\hat{p}_{\uparrow}(z,t)$ and $\hat{p}_{\downarrow}(z,t)$ associate with the coherence between the states $|s\rangle$ and $|\uparrow\rangle$ and the coherence between $|s\rangle$ and $|\downarrow\rangle$, respectively. When
the reading beam is turned on, $\tilde{R}_1(z,t)$ and $\tilde{R}_2(z,t)$ will be converted into the left- and right-circularly polarized optical fields $\tilde{e}_\downarrow(z,t)$ and $\tilde{e}_\uparrow(z,t)$, respectively. Such conversions can be described by the two-state dark-polaritons (DSPs) [16,17]:

$$\Psi_+(z,t) = \cos \vartheta_+(t)\tilde{e}_+(z,t) - \sin \vartheta_+(t)\sqrt{N}\tilde{R}_1(z,t),$$  
$$\Psi_-(z,t) = \cos \vartheta_-(t)\tilde{e}_-(z,t) - \sin \vartheta_-(t)\sqrt{N}\tilde{R}_2(z,t),$$  

where $\vartheta_+(t) = \sqrt{N}g_\downarrow/\Omega_C$; $\Omega_C$ is the Rabi frequency of the (reading) coupling beam, $N$ represents the atomic numbers, $g_\downarrow = \mu_+\sqrt{v/2\hbar\epsilon_0}$ and $g_\uparrow = \mu_-\sqrt{v/2\hbar\epsilon_0}$ are the atomic-field coupling constants for the $|\uparrow\rangle \leftrightarrow |\downarrow\rangle$ transitions, $\mu_+ (\mu_-)$ is the dipole moment of the $|\uparrow\rangle \leftrightarrow |\uparrow\rangle$ ($|\downarrow\rangle \leftrightarrow |\downarrow\rangle$) transition, $v$ is the carrier frequency of the optical signal field, and $V$ is the quantization volume.

In the presented atomic system, the transitions $|\downarrow\rangle \leftrightarrow |\downarrow\rangle$ and $|\uparrow\rangle \leftrightarrow |\uparrow\rangle$ are symmetric, so $\mu_+ = \mu_-$, $g_\downarrow = g_\uparrow$, and $\vartheta_+(t) = \tan \vartheta_-(t) = \tan \vartheta_-$. Further, we can define

$$\Psi(z,t) = \alpha_0\Psi_+(z,t) + e^{-i\Delta t}\beta\Psi_-(z,t) = \cos \vartheta_+(t)\tilde{e}(z,t) - \sin \vartheta(t)\sqrt{N}\tilde{R}(z,t),$$

as the two-state polariton operator [17], where the optical field $\tilde{e}(z,t) = \alpha\tilde{e}_+(z,t) + e^{-i\Delta t}\beta\tilde{e}_-(z,t)$ is the superposition of the two optical fields $\tilde{e}_+(z,t)$ and $\tilde{e}_-(z,t)$. Such that two-state polariton describes the conversion of the optical field $\tilde{e}(z,t)$ and spin wave $\tilde{R}(z,t)$ in the four-level system. Actually, the definition of two-state polariton includes two spin-wave operators $\tilde{R}_1(z,t)$ and $\tilde{R}_2(z,t)$ $[\tilde{R}_1(z,t), \tilde{R}_2(z,t)] = i\alpha\tilde{R}_1(z,t) + e^{-i\Delta t}\beta\tilde{R}_2(z,t)$, which are similar to that of the generalized dark-state polaritons [18,19]. All the number states created by $\Psi(z,t)$ are dark states: $|D_\pm^\pm\rangle = (\sqrt{n})^{-\frac{1}{2}}\{\Psi(z,t)\}^0\Phi_+ \pm \Phi_-$, where $\Psi(t)$ is the plane-wave decomposition of $\tilde{e}(z,t) = \sum_k \Psi_k(t)e^{i\vec{k}\cdot\vec{r}}$ [16].

Since the spin-coherence operators $\tilde{\rho}_1(z,t)$ and $\tilde{\rho}_2(z,t)$ are orthogonal to each other $[\tilde{\rho}_1(z,t), \tilde{\rho}_2(z,t)] = 0$, they form a spin-coherence basis $\{|\uparrow\rangle\langle\uparrow|\}$ and $\{|\downarrow\rangle\langle\downarrow|\}$. In this basis, the spin wave can be rewritten as a vector: $\hat{S}_\Phi(z,t) = (\langle\tilde{\rho}_\Phi(z,t)\rangle\hat{S}_\Phi = (\langle\tilde{\rho}_\Phi(z,t)\rangle)(\alpha\hat{S}_\uparrow + e^{-i\Delta t}\beta\hat{S}_\downarrow)$, where $\langle\tilde{\rho}_\Phi(z,t)\rangle$ is the expectation value of the spin wave, and is given by $\langle\tilde{\rho}_\Phi(z,t)\rangle = \langle\sqrt{\tilde{R}_1(z,t)}\sqrt{\tilde{R}_2(z,t)}\rangle = \sqrt{\tilde{R}_1(z,t)}$ (the population in the state $|\uparrow\rangle$) [16], $\delta_\Phi = (N^*)^{-1}\sum_{j=1}^{N^*}|s_j\rangle\langle\Phi|$ and $\delta_\uparrow = (N^*)^{-1}\sum_{j=1}^{N^*}|s_j\rangle\langle\uparrow|$ $(l = \uparrow, \downarrow)$ is the basis vector. With the projections of the basis vector $\langle\tilde{\rho}_\Phi(z,t)\rangle = \langle\tilde{\rho}_\uparrow(z,t)\rangle = \langle\tilde{\rho}_\downarrow(z,t)\rangle = 1$ (where $l = \sum_{j=1}^{N^*}|s_j\rangle\langle l|$), we can calculate the projections of spin wave on the basis vectors: $\langle\tilde{S}_\Phi(z,t)|\Phi\rangle = (\langle\tilde{\rho}_\Phi(z,t)\rangle)$, $\langle\tilde{S}_\Phi(z,t)|\uparrow\rangle = \alpha\langle\tilde{\rho}_\Phi(z,t)\rangle\langle\uparrow\rangle$, $\langle\tilde{S}_\Phi(z,t)|\downarrow\rangle = e^{-i\Delta t}\beta\langle\tilde{\rho}_\Phi(z,t)\rangle\langle\downarrow\rangle$. Writing the basis unit vectors as $\hat{S}_\uparrow = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ and $\hat{S}_\downarrow = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$, the spin-wave vector can be rewritten as

$$\hat{S}_\Phi(z,t) = (\langle\tilde{\rho}_\Phi(z,t)\rangle)\begin{pmatrix} \alpha \\ 0 \end{pmatrix},$$

which can be regarded as the superposition of the two orthogonal spin-wave components

$$\hat{S}_\uparrow(z,t) = (\langle\tilde{\rho}_\Phi(z,t)\rangle)\begin{pmatrix} \alpha \\ 0 \end{pmatrix},$$
$$\hat{S}_\downarrow(z,t) = (\langle\tilde{\rho}_\Phi(z,t)\rangle)\begin{pmatrix} 0 \\ 0 \end{pmatrix},$$

$\hat{S}_\uparrow(z,t)$ and $\hat{S}_\downarrow(z,t)$ will be converted to left- and right-circularly $(\sigma^+)$ and $\sigma^-$) polarized optical fields $e^{\text{out}}_\uparrow(z,t)$, respectively, when a reading beam is used for reading the spin waves. Considering the retrieval efficiency, the retrieved optical field is

$$e^{\text{out}}_\uparrow(z,t) = (\langle\tilde{\rho}_\Phi(z,t)\rangle)\begin{pmatrix} \alpha \\ 0 \end{pmatrix},$$

where $\eta_1$ is the retrieval efficiency from the channel $\hat{S}_\uparrow(z,t)$ $[\hat{S}_\uparrow(z,t)]$. The retrieval efficiency $\eta_1$ is proportional to the optical depth [20] of the transition $|\uparrow\rangle \leftrightarrow |e\rangle$ and $|\downarrow\rangle \leftrightarrow |e\rangle$. Since the transitions $|\uparrow\rangle \leftrightarrow |e\rangle$ and $|\downarrow\rangle \leftrightarrow |e\rangle$ are symmetric, so $\eta_1 = \eta_1$. Thus we have

$$\begin{pmatrix} e^{\text{out}}_\uparrow(z,t) \\ e^{\text{out}}_\downarrow(z,t) \end{pmatrix} = \sqrt{\eta_1}\begin{pmatrix} \alpha \\ -\alpha \end{pmatrix},$$

It is obvious that the readout field $e^{\text{out}}(z,t)$ directly copies the polarization information of the spin-wave vector.

We now explain why the $R(\vartheta_\Phi)$ and $R(\Delta\Phi)$ rotation of the spin-wave vector $\tilde{S}_\Phi(z,t)$ on the Bloch sphere can be implemented by means of Raman two-photon transition and controllable Larmor spin precession. In the presented scheme, we first prepare all the atoms in the ground state $|\uparrow\rangle$, and then create the spin wave $\tilde{S}_\uparrow$ by storing a weak left-circularly polarized optical signal into the atoms. So, we have the initial conditions $\Phi(0) = |\uparrow\rangle$ and

$$\hat{S}_\Phi(z,0) = (\langle\tilde{\rho}_\Phi(z,0)\rangle)\begin{pmatrix} 1 \\ 0 \end{pmatrix} = (\langle\tilde{\rho}_\uparrow(z,0)\rangle)\begin{pmatrix} 1 \\ 0 \end{pmatrix}.$$
two-photon transition. The Raman laser beam consists of $\sigma^+$- and $\sigma^-$-polarized light fields $E_{R^+}$ and $E_{R^-}$, which couple to $|\uparrow\rangle \leftrightarrow |e\rangle$ and $|\downarrow\rangle \leftrightarrow |e\rangle$ transitions, respectively, with a two-photon detuning $\delta_R \approx 0$ and a larger single-photon detuning $\Delta_R$ [see Fig. 1(b)]. If both the nature width $\Gamma$ and the Rabi frequencies $\Omega_{R^\pm} = \mu_{\pm} E_{R^\pm}/\hbar$ are significantly smaller than the detuning $\Delta_R$, the upper state $|e\rangle$ is adiabatically eliminated, and the effective interaction Hamiltonian is given by $H_{\text{eff}} = -h/2 \sum_{n=1}^{N} (\Omega_R | \uparrow\rangle \langle \downarrow| + \text{H.c.})$, where $\Omega_R = \Omega_R^+ + \Omega_R^-/2 \Delta_R$ is the Raman-Rabi frequency. From the Hamiltonian $H_{\text{eff}}$, we obtain the solutions of the superposition state $\Phi(t)$ for an atom and then solve the evolution equation of the spin wave $\hat{S}_{\phi}(z,t)$, which can be described by a unitary Raman rotation $R(\theta, \varphi)$ and we have $R(\theta, \varphi) \hat{S}_{\phi}(z,0) \rightarrow \hat{S}_{\phi}(z,t)$, where

$$ R(\theta, \varphi) = \begin{pmatrix} \cos \frac{\theta}{2} & -i e^{i \varphi} \sin \frac{\theta}{2} \\ -i e^{-i \varphi} \sin \frac{\theta}{2} & \cos \frac{\theta}{2} \end{pmatrix}, $$

$\theta = \Omega_g t$, and $\varphi = \varphi_+ - \varphi_-$ is the phase difference between $\sigma^+$ and $\sigma^-$ Raman fields $E_{R^+}$ and $E_{R^-}$. In the following we will discuss why the relative phase $\Delta$ can be controllably changed by Larmor precession. In a magnetic field, the two spin-wave components $\hat{S}_{\phi}(z,t)$ and $\hat{S}_{\psi_1}(z,t)$ experience Larmor precession [19] and get phase shifts $\varphi_1$ and $\varphi_2$, respectively, which introduce a relative phase $\phi = \varphi_1 - \varphi_2$ after an evolution time interval $t$. The evolution of the spin wave is described by

$$ \hat{S}_{\phi}(z,t) = R(\phi_2) \hat{S}_{\phi}(z,0) = \langle |\hat{\rho}_{\phi_2}(z,0)| \rangle \begin{pmatrix} \alpha e^{i \phi} \\ \beta \end{pmatrix}, $$

where

$$ R(\phi_2) = \begin{pmatrix} 1 & 0 \\ 0 & e^{i \phi} \end{pmatrix} $$

is the matrix rotation and the initial spin wave is assumed to be

$$ \hat{S}_{\phi}(z,0) = \langle |\hat{\rho}_{\phi}(z,0)| \rangle \begin{pmatrix} \alpha \\ \beta \end{pmatrix}. $$

It is obvious that the spin wave acquire a relative phase $\Delta = \phi_2$ due to Larmor precession.

### III. EXPERIMENTAL SETUP

The experimental setup is shown in Fig. 1(d). A cold $^{87}$Rb atomic cloud released from a magneto-optical trap (MOT) serves as the atomic ensemble. The measured optical depth of the cold atoms is $\sim 1.5$ and the trap temperature can reach $\sim 200 \mu$K. A 780-nm $\sigma^-$-polarized pumping laser couples to the transition $|S^2S_{1/2},F = 1\rangle \leftrightarrow |S^2P_{3/2},F' = 1\rangle$ to prepare atoms into $|\downarrow\rangle$ state. The $\sigma^+$-polarized input optical signal field $\hat{E}_{\phi}(z,t)$ (with a power of $\sim 17 \mu$W and a diameter of $\sim 2.6$ mm) is tuned to the transition $|\uparrow\rangle \leftrightarrow |e\rangle$, and goes through cold atoms along the $z$ axis. The $\sigma^+$-polarized writing beam $W$ (with a power of $\sim 1$ mW and a diameter of 2.5 mm) is tuned to the transition $|\uparrow\rangle \leftrightarrow |e\rangle$ and goes through the cold atoms with a small angle of $\sim 0.5^\circ$ from the $x$ axis. The linearly polarized Raman laser beam (with a $\sim 5.2$ mm diameter) passing through the cold atoms with an angle of $\sim 1^\circ$ from the $z$ axis provides $\sigma^+$- and $\sigma^-$-polarized Raman fields $E_{R^+}$ and $E_{R^-}$, which respectively couple to the transitions $|\uparrow\rangle \leftrightarrow |e\rangle$ and $|\downarrow\rangle \leftrightarrow |e\rangle$ with a detuning $\Delta_R \approx 90$ MHz. We use an analog acousto-optic modulator (AOM) to modulate Raman laser amplitude and then obtain a Gaussian-shape pulse with a time width of 2.1 $\mu$s. A $\sigma^+$-polarized reading beam (with a power of $\sim 17.7$ mW and a $\sim 2.8$ mm diameter) couples to the transitions $|\downarrow\rangle \leftrightarrow |e\rangle$ to retrieve the two spin-wave components $\hat{S}_{\phi}(z,t)$ and $\hat{S}_{\psi_1}(z,t)$. In the experiment, the MOT is switched off, and at the same time, a dc magnetic field $B_0$ of $\sim 300$ mG along the $z$ axis is applied, so the $z$ direction quantization axis is well defined. Then the 780-nm pumping and the $\sigma^+$-polarized writing laser beams are turned on to prepare the atoms into the single Zeeman state $|\uparrow\rangle$. After 300 $\mu$s, the $\sigma^+$-polarized probe pulse (with a pulse length of 200 ns) is turned on. By switching off the $\sigma^+$-writing laser beams at time $t = 0$, the signal field is stored into the atomic ensemble and creates an initial spin wave $\hat{S}_{\phi}(z,0) = \langle |\hat{\rho}_{\phi}(z,0)| \rangle \begin{pmatrix} 1 \\ 0 \end{pmatrix}$.

The stored spin wave will be unitarily transformed into

$$ \hat{S}_{\phi}(z,t) = \langle |\hat{\rho}_{\phi}(z,t)| \rangle \begin{pmatrix} \alpha e^{-i \Delta R} \\ \beta \end{pmatrix} $$

by Raman manipulation and/or Larmor precession and then is retrieved at time $t$. During the reading process, the two spin-wave components $\hat{S}_{\phi}(z,t)$ and $\hat{S}_{\psi_1}(z,t)$ are converted into the $\sigma^+$- and $\sigma^-$-polarized output optical signal fields $\epsilon_{\text{out}}^+$ and $\epsilon_{\text{out}}^-$, respectively. After passing through a $\lambda/4$-wave plate, $\epsilon_{\text{out}}^+$ and $\epsilon_{\text{out}}^-$ will become vertical and horizontal polarizations, respectively, and then are split by a polarization beam splitter (PBS). The separated $\epsilon_{\text{out}}^+$ and $\epsilon_{\text{out}}^-$ signals are detected by D1 and D2 detectors, respectively.

### IV. RESULTS AND DISCUSSION

To perform a spin wave $R(\theta, \varphi)$ rotation induced by Raman laser pulse, we first observe the population transfer from $\hat{S}_{\phi}(z,t)$ and $\hat{S}_{\psi_1}(z,t)$ components as the function of the rotation angle $\theta$. Curves ($+$) and ($-$) in Fig. 2(a) show the retrieved signals $\epsilon_{\text{out}}^+(t)$ and $\epsilon_{\text{out}}^-(t)$ from the stored spin wave

$$ \hat{S}_{\phi}(z,t) = \langle |\hat{\rho}_{\phi}(z,t)| \rangle \begin{pmatrix} 1 \\ 0 \end{pmatrix} $$

at $t = 17 \mu$s when the Raman laser beam is not applied. It can be seen that there is only $\epsilon_{\text{out}}^+$ readout signal [curve ($+$)] and no $\epsilon_{\text{out}}^-$ readout signal [curve ($-$)], which means that the spin coherence does not freely exchange between $\hat{S}_{\phi}(z,t)$ and $\hat{S}_{\psi_1}(z,t)$ channels. Curves ($+$) and ($-$) in Fig. 2(b) exhibit the retrieved signals $\epsilon_{\text{out}}^+$ and $\epsilon_{\text{out}}^-$ simultaneously while a linearly polarized Raman laser pulse with a peak power $P_R = 77$ mW and a pulse width $\tau_R = 2.1 \mu$s is applied. The results show that the spin wave is flipped, which corresponds to a $\pi$-pulse operation. To describe the relative value of readout fields $\epsilon_{\text{out}}^+(t)$ and $\epsilon_{\text{out}}^-(t)$ to the original $\epsilon_{\text{out}}^0(t)$ readout, we defined a normalized retrieval efficiency $N_k = \int |\epsilon_{\text{out}}(t)|^2 dt / \int |\epsilon_{\text{out}}^0(t)|^2 dt$, where $\int |\epsilon_{\text{out}}(t)|^2 dt$ corresponds to the retrieved photon numbers from the spin wave without experiencing Raman laser manipulation at $t = 17 \mu$s. The square (circle) points in Fig. 2(c) present the...
FIG. 2. (Color online) The coherence population transfer between the spin-wave components $\hat{S}_{+1}(z,t)$ and $\hat{S}_{-1}(z,t)$. The curves (+) and (−) in (a) and (b) are the retrieved signal from $\hat{S}_{+1}(z,t)$ and $\hat{S}_{-1}(z,t)$ respectively. (a) is without Raman laser pulse; (b) is with Raman pulse. The square and circle dots in (c) are the measured normalized retrieval efficiency $N_+$ and $N_-$ as the function of $\Omega_R$. The solid lines are sinusoidal fits to the data.

normalized retrieval efficiencies $N_+$ ($N_-$) as the function of Raman-Rabi frequency $\Omega_R$. The solid curves in Fig. 2(c) are the fits to the experimental data based on functions $[1 \pm \cos(2\pi \Omega_R t_\phi)]/2$, with the parameter $B = 0.82$. The fits present sinusoidal Rabi oscillations which are consistent with the theoretical predictions $N_\pm = [1 \pm \cos(2\pi \Omega_R t_\phi)]/2$. At $\theta = 2\pi B \Omega_R t_\phi = \pi$ [see upper axis in Fig. 2(c)], the population transfer efficiency reaches ~97%.

We then measure the phase $\psi$ in the rotation $\mathbf{R}(\theta, \phi)$ induced by Raman laser manipulation. The relationship between $\psi$ and the orientation angle $\phi_R$ of the linearly polarized Raman laser is $\psi = -\pi/2 - 2\phi_R$ ($\phi_R = 0$ corresponding to the vertical polarization). By applying a $\pi/2$ Raman pulse with a variable $\phi_R$, we transform the initial spin wave $\hat{s}_\phi(z,0)$ into

$$\hat{s}_\phi(z,t) = \frac{\langle |\hat{\rho}_{11}(z,0)| \rangle}{\sqrt{2}} \left( e^{i\phi_R} \right).$$

After a storage time $t = 17 \mu s$, the spin wave evolves to

$$\hat{s}_\phi(z,t) = \frac{\langle |\hat{\rho}_{11}(z,0)| \rangle}{\sqrt{2}} \left( e^{i\phi_R} \right).$$

due to Larmor precession in the dc magnetic field $B_0$ and we turn on the $\sigma^+$-polarized reading beam to read the $\hat{S}_{+1}(z,t)$ and $\hat{S}_{-1}(z,t)$. A movable half-wave plate is inserted in front of the PBS to rotate vertically polarized $e^\text{out}$ and horizontally polarized $e^\text{out}$ fields by 45°, respectively. Thus, D1 and D2 detect the fields $e^\text{out}_{45+} = (e^\text{out}_+ + e^\text{out}_-)/\sqrt{2}$ and $e^\text{out}_{45-} = (e^\text{out}_+ - e^\text{out}_-)/\sqrt{2}$ at ±45° orientation, and generate the output $\langle |e^\text{out}_{45\pm}|^2 \rangle = [\langle |e^\text{out}_+ + e^\text{out}_-|^2 \rangle]/2 \propto [1 \pm \cos(2\phi_R + \phi_{\phi_0})]/2$, respectively. Figure 3(a) presents the relative retrieved efficiencies $N_{\pm 45}$ ($N_{\pm 45} = [\langle |e^\text{out}_{45\pm}|^2 \rangle/\langle |e^\text{out}_{45\mp}|^2 \rangle]$ as the function of $\phi_R$. The solid lines are fits to the experimental data using functions $[a \pm b \cos(2\phi_R)]/2$, with parameters $\phi_{\phi_0} = 0, a = 0.96$, and contrast $b = 0.96$.

By applying a variable field of the magnetic pulse $B(t)$ to the atomic ensemble, we implement spin-wave phase operation, i.e.,

$$R_\phi(\phi_\tau) = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\phi_\tau} \end{pmatrix}. $$

rotation. The relative phase shift between $\hat{S}_{+1}(z,t)$ and $\hat{S}_{-1}(z,t)$ components induced by Larmor precession in the magnetic field $B = B_0 + B(t)$ can be written as $\phi_R = \phi_{\phi_0} + \Delta\phi_2$, where $\phi_{\phi_0}$ is the phase shift induced by the dc magnetic field $B_0$ ($\sim 300$ mG) and $\Delta\phi_2 \approx \int B(t)dt$ is the phase shift induced by the pulsed magnetic field $B(t)$. We apply a current pulse $I(t)$ to a pair of coils, C1 and C2, to generate the pulsed magnetic field $B(t)$. The generated pulsed magnetic field $B(t)$ is proportional to $I(t)$. By changing the area $\int I(t)dt$ of current pulse, we can control the changes of $\Delta\phi_2$ and then implement the $R_2(\Delta\phi_2)$ rotation. By observing the interference fringe between the readout fields $e^\text{out}(t)$ and $e^\text{out}(t)$, we verify the implementation of the $R_2(\Delta\phi_2)$ rotation. In the experiment, we apply a $\pi/2$ linearly polarized Raman laser pulse (with an orientation angle $\phi_R = 8^\circ$) firstly and then apply a magnetic pulse with a duration of $\tau \sim 7 \mu s$ to rotate the initial spin wave $\hat{s}_\phi(z,0)$. After these operations, the spin wave evolves to

$$\hat{s}_\phi(z,t) = \frac{\langle |\hat{\rho}_{11}(z,0)| \rangle}{\sqrt{2}} \left( e^{i\Delta\phi_0 + i\phi_\tau} \right).$$

where $\Delta_0 = -\pi/2 - \psi + \phi_{\phi_0}$ is kept unchanged. At $t = 17 \mu s$, we tuned on the reading beam to read the spin wave. Figure 3(b) plots the relative retrieved efficiencies $N_{\pm 45}$ (square and circle dots) as the function of the relative magnetic pulse area $A$ [21]. The solid lines are the fits to the measured data $N_{\pm 45}$ using sinusoidal functions $[a \pm b \cos(2\pi A)]/2$, with parameters $\Delta_0 = 0, a = 0.93$, and contrast $b = 0.93$. The magnetic pulse width is ~7 $\mu s$ in the presented experiment; we believe that it can be further decreased by improving the coils and the current pulse source.
FIG. 4. (Color online) Ramsey fringes for a pair of $\pi/2$ pulses with a variable separate time $\tau_R$. Red circular points (blue square points): the normalized retrieval efficiency $N_+$ ($N_-$). The solid lines are sinusoidal fits to the data.

To estimate the $\pi/2$-pulse fidelity, we perform a Ramsey experiment by applying two linearly polarized $\pi/2$ Raman laser pulses with a variable time interval $\tau_R$. At $t = 17 \mu$s, we retrieve the spin wave $\tilde{\delta}_\phi(z,t)$ into readout signal fields $\tilde{\varepsilon}_\pm$. When the movable $\lambda/2$-wave plate is removed, the readouts $\epsilon_\pm$ signals are injected into D1 and D2, respectively. Figure 4 plots the measured relative photon numbers $N_\pm$ as the function of interval $\tau_R$. The solid lines are the fits to the data $N_\pm$ using the sinusoid function $(1 \pm b_\pm \cos 2\pi \tau_R/T_L)/2$, with the Larmor period $T_L = 2.82 \times 10^{-6}$ s, and contrasts $b_+ = 1$ for $N_+$ as well as $b_- = 0.85$ for $N_-$. We consider that the difference between $b_+$ and $b_-$ results from the imprecisely Raman laser power for the $\pi/2$ pulse. According to Ref. [13], we calculate the $\pi/2$ fidelity of $F_{\pi/2} = (1 + \sqrt{b})/2 \approx 96\%$ by using the lower value of contrast ($b_-$). We believe that $F_{\pi/2}$ can be further improved by more precisely adjusting the Raman laser power to obtain a perfect $\pi/2$-pulse operation.

\section*{V. CONCLUSION}

We demonstrated the $R(\theta, \phi)$ and $R_\tau(\Delta \phi)$ rotations of spin-wave vector on the Bloch sphere by applying Raman laser and magnetic field pulses. With the reading beam turned on, the two spin-wave components are converted into two orthogonal polarized optical emissions, respectively. By detecting the two orthogonal polarized optical emissions, the populations of two spin-wave components and their relative phase are measured. The time scale of the $\pi$-pulse operation or phase gate operation on the spin waves is approximately several microseconds in the presented experiment, while the decoherence (storage) time of the spin waves is approximately several tens of microseconds [19]. So the storage time of the spin waves is approximately ten times longer than the gate operation time. We believe that by further suppressing the decay of the spin waves, as well as shortening the width of the Raman laser and magnetic field pulses, many more gate operations can be executed within the storage time of the spin waves based on the presented scheme. When the initially stored spin wave has one atomic collective excitation (i.e., $N \int \langle \hat{\rho}_z(z,0)\hat{\rho}_z^\dagger(z,0) \rangle dz = 1$), the two spin-wave components will share one excitation and may serve as two basis states of a qubit. Thus the manipulation demonstrated in the presented work can be used for implementing a single-qubit gate operation, which has potential applications in QIP based on atomic ensemble.

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[21] The relative magnetic pulse area is $A = \int B(t)dt/\int B_0(t)dt$. According to the relation $B(t) \propto l(t)$, we have $A = \int l(t)dt/\int l_0(t)dt$, meaning we can obtain the values $A$ by measuring the values $l(t)$. In Fig. 3(b), $A$ is the area of the current pulse normalized to the current pulse area $\int l_0(t)dt$, where $\int l_0(t)dt$ is the right end of the A axis and has been set to 1.